

PROPERTIES OF MEDIAN GRAPHS

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A characterization of some proper class of the median graphs which are defined recursively is given. It is known that the median graphs are exactly retracts of hypercubes [1] and they have the fixed hypercube property under edge-preserving maps [2]. An elementary retraction of the median graph it is defined and it is shown that any c-recursively median graph is retractible. There are some similarities between c-recursively median graphs, defined in our paper, and s-recursively contractible complexes [3]. The s-recursively contractible complexes are a special class of retractible complexes and they have a fixed simplex property [4]. Moreover, it is possible to obtain any hypercube contained in a c-recursively median graph by elementary retractions. An alternative proof of the fixed hypercube property for c-recursively median graphs is presented.

References

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