PRODUCT-IRREGULAR LABELINGS OF GRAPHS

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Consider a simple graph $G$ with no isolated edges and at most one isolated vertex. A labeling $w : E(G) \to \{1, 2, \ldots, m\}$ is called product - irregular, if all product degrees $pd_{G}(v) = \prod_{e \ni v} w(e)$ are distinct. The goal is to obtain a product - irregular labeling that minimizes the maximal label. This minimal value is called the product irregularity strength and denoted $ps(G)$. One may also consider some variants of $ps(G)$, as e.g. its local version or the situation when vertex labeling is also allowed.

We consider product-irregular labelings of graphs from several families, as e.g. complete graphs, some graphs with $\delta(G) = 1$ and some families of trees.

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